

Product & Quotient Rules

Product Rule:

The derivative of $f(x)g(x)$ is $f'(x)g(x) + f(x)g'(x)$

1. $f(x) = x^2 e^x$

$$f'(x) = 2x e^x + x^2 e^x$$

$$f'(x) = x e^x (2 + x)$$

2. $f(x) = 2x^{1/2}(3x-1)$

$$f'(x) = x^{-1/2}(3x-1) + (2x^{1/2})(3)$$

$$f'(x) = \frac{3x-1}{x^{1/2}} + 6x^{1/2}$$

3. $f(x) = (\frac{2}{3}x^3 + 6x - 2)(4\sqrt{x} - 6)$

$$f'(x) = (2x^2 + 6)(4x^{1/2} - 6) + (\frac{2}{3}x^3 + 6x - 2)(2x^{-1/2})$$

$$f'(x) = (2x^2 + 6)(4x^{1/2} - 6) + (\frac{2}{3}x^3 + 6x - 2)(\frac{2}{x^{1/2}})$$

Quotient Rule:

The derivative of $\frac{f(x)}{g(x)}$ is $\frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2}$

1. $f(x) = \frac{x^2 + 3}{x^2 - 4}$

$$f'(x) = \frac{(2x)(x^2 - 4) - (x^2 + 3)(2x)}{(x^2 - 4)^2}$$

$$f'(x) = \frac{2x^3 - 8x + [-2x^3 - 6x]}{(x^2 - 4)^2}$$

$$f'(x) = \frac{-14x}{(x^2 - 4)^2}$$

2. $f(x) = \frac{x+1}{x^2 + 2x + 2}$

$$f'(x) = \frac{(1)(x^2 + 2x + 2) - (x+1)(2x+2)}{(x^2 + 2x + 2)^2}$$

$$f'(x) = \frac{x^2 + 2x + 2 + [-2x^2 - 2x - 2x - 2]}{(x^2 + 2x + 2)^2}$$

$$f'(x) = \frac{-x^2 - 2x}{(x^2 + 2x + 2)^2} = \frac{-x(x+2)}{(x^2 + 2x + 2)^2}$$

3. $f(x) = \left(\frac{x+4}{x+3}\right)(2x+5) = \frac{2x^2 + 13x + 20}{x+3}$

$$f'(x) = \frac{(4x+13)(x+3) + (2x^2 + 13x + 20)(1)}{(x+3)^2}$$

$$f'(x) = \frac{4x^2 + 12x + 13x + 39 - 2x^2 - 13x - 20}{(x+3)^2}$$

$$f'(x) = \frac{2x^2 + 12x + 19}{(x+3)^2}$$

4. $f(x) = \frac{x^2 + c^2}{x^2 - c^2}$ * c is a constant

$$f'(x) = \frac{(2x)(x^2 - c^2) - (x^2 + c^2)(2x)}{(x^2 - c^2)^2}$$

$$f'(x) = \frac{2x^3 - 2c^2x + [-2x^3 - 2c^2x]}{(x^2 - c^2)^2}$$

$$f'(x) = \frac{-4c^2x}{(x^2 - c^2)^2}$$